

## 0.1 normal: Normal Regression for Continuous Dependent Variables

The Normal regression model is a close variant of the more standard least squares regression model (see Section ??). Both models specify a continuous dependent variable as a linear function of a set of explanatory variables. The Normal model reports maximum likelihood (rather than least squares) estimates. The two models differ only in their estimate for the stochastic parameter  $\sigma$ .

### Syntax

```
> z.out <- zelig(Y ~ X1 + X2, model = "normal", data = mydata)
> x.out <- setx(z.out)
> s.out <- sim(z.out, x = x.out)
```

### Additional Inputs

In addition to the standard inputs, `zelig()` takes the following additional options for normal regression:

- **robust**: defaults to **FALSE**. If **TRUE** is selected, `zelig()` computes robust standard errors via the `sandwich` package (see Zeileis (2004)). The default type of robust standard error is heteroskedastic and autocorrelation consistent (HAC), and assumes that observations are ordered by time index.

In addition, **robust** may be a list with the following options:

- **method**: Choose from
  - \* **"vcovHAC"**: (default if **robust** = **TRUE**) HAC standard errors.
  - \* **"kernHAC"**: HAC standard errors using the weights given in Andrews (1991).
  - \* **"weave"**: HAC standard errors using the weights given in Lumley and Heagerty (1999).
- **order.by**: defaults to **NULL** (the observations are chronologically ordered as in the original data). Optionally, you may specify a vector of weights (either as **order.by** = **z**, where **z** exists outside the data frame; or as **order.by** = **~z**, where **z** is a variable in the data frame). The observations are chronologically ordered by the size of **z**.
- **...**: additional options passed to the functions specified in **method**. See the `sandwich` library and Zeileis (2004) for more options.

### Examples

1. Basic Example with First Differences

Attach sample data:

```
> data(macro)
```

Estimate model:

```
> z.out1 <- zelig(unem ~ gdp + capmob + trade, model = "normal",  
+ data = macro)
```

Summarize of regression coefficients:

```
> summary(z.out1)
```

Set explanatory variables to their default (mean/mode) values, with high (80th percentile) and low (20th percentile) values for trade:

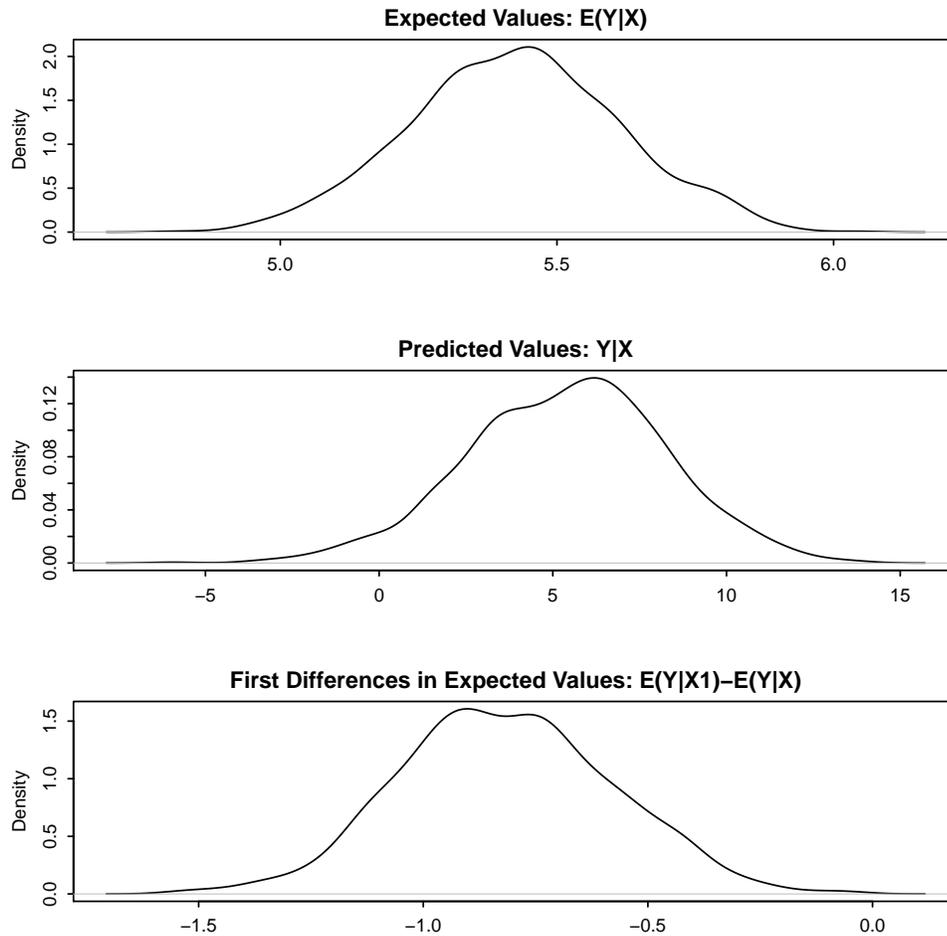
```
> x.high <- setx(z.out1, trade = quantile(macro$trade, 0.8))  
> x.low <- setx(z.out1, trade = quantile(macro$trade, 0.2))
```

Generate first differences for the effect of high versus low trade on GDP:

```
> s.out1 <- sim(z.out1, x = x.high, x1 = x.low)  
  
> summary(s.out1)
```

A visual summary of quantities of interest:

```
> plot(s.out1)
```



## 2. Using Dummy Variables

Estimate a model with a dummy variable for each year and country (see ?? for help with dummy variables). Note that you do not need to create dummy variables, as the program will automatically parse the unique values in the selected variables into dummy variables.

```
> z.out2 <- zelig(unem ~ gdp + trade + capmob + as.factor(year) +
+   as.factor(country), model = "normal", data = macro)
```

Set values for the explanatory variables, using the default mean/mode variables, with country set to the United States and Japan, respectively: Simulate quantities of interest:

## Model

Let  $Y_i$  be the continuous dependent variable for observation  $i$ .

- The *stochastic component* is described by a univariate normal model with a vector of means  $\mu_i$  and scalar variance  $\sigma^2$ :

$$Y_i \sim \text{Normal}(\mu_i, \sigma^2).$$

- The *systematic component* is

$$\mu_i = x_i\beta,$$

where  $x_i$  is the vector of  $k$  explanatory variables and  $\beta$  is the vector of coefficients.

## Quantities of Interest

- The expected value (`qi$ev`) is the mean of simulations from the the stochastic component,

$$E(Y) = \mu_i = x_i\beta,$$

given a draw of  $\beta$  from its posterior.

- The predicted value (`qi$pr`) is drawn from the distribution defined by the set of parameters  $(\mu_i, \sigma)$ .
- The first difference (`qi$fd`) is:

$$\text{FD} = E(Y | x_1) - E(Y | x)$$

- In conditional prediction models, the average expected treatment effect (`att.ev`) for the treatment group is

$$\frac{1}{\sum_{i=1}^n t_i} \sum_{i:t_i=1}^n \{Y_i(t_i = 1) - E[Y_i(t_i = 0)]\},$$

where  $t_i$  is a binary explanatory variable defining the treatment ( $t_i = 1$ ) and control ( $t_i = 0$ ) groups. Variation in the simulations are due to uncertainty in simulating  $E[Y_i(t_i = 0)]$ , the counterfactual expected value of  $Y_i$  for observations in the treatment group, under the assumption that everything stays the same except that the treatment indicator is switched to  $t_i = 0$ .

- In conditional prediction models, the average predicted treatment effect (`att.pr`) for the treatment group is

$$\frac{1}{\sum_{i=1}^n t_i} \sum_{i:t_i=1}^n \left\{ Y_i(t_i = 1) - \widehat{Y_i(t_i = 0)} \right\},$$

where  $t_i$  is a binary explanatory variable defining the treatment ( $t_i = 1$ ) and control ( $t_i = 0$ ) groups. Variation in the simulations are due to uncertainty in simulating  $\widehat{Y_i(t_i = 0)}$ , the counterfactual predicted value of  $Y_i$  for observations in the treatment group, under the assumption that everything stays the same except that the treatment indicator is switched to  $t_i = 0$ .

## Output Values

The output of each Zelig command contains useful information which you may view. For example, if you run `z.out <- zelig(y ~ x, model = "normal", data)`, then you may examine the available information in `z.out` by using `names(z.out)`, see the `coefficients` by using `z.out$coefficients`, and a default summary of information through `summary(z.out)`. Other elements available through the `$` operator are listed below.

- From the `zelig()` output object `z.out`, you may extract:
  - `coefficients`: parameter estimates for the explanatory variables.
  - `residuals`: the working residuals in the final iteration of the IWLS fit.
  - `fitted.values`: fitted values. For the normal model, these are identical to the linear predictors.
  - `linear.predictors`: fitted values. For the normal model, these are identical to `fitted.values`.
  - `aic`: Akaike's Information Criterion (minus twice the maximized log-likelihood plus twice the number of coefficients).
  - `df.residual`: the residual degrees of freedom.
  - `df.null`: the residual degrees of freedom for the null model.
  - `zelig.data`: the input data frame if `save.data = TRUE`.
- From `summary(z.out)`, you may extract:
  - `coefficients`: the parameter estimates with their associated standard errors,  $p$ -values, and  $t$ -statistics.
  - `cov.scaled`: a  $k \times k$  matrix of scaled covariances.
  - `cov.unscaled`: a  $k \times k$  matrix of unscaled covariances.
- From the `sim()` output object `s.out`, you may extract quantities of interest arranged as matrices indexed by simulation  $\times$   $x$ -observation (for more than one  $x$ -observation). Available quantities are:
  - `qi$ev`: the simulated expected values for the specified values of  $x$ .
  - `qi$pr`: the simulated predicted values drawn from the distribution defined by  $(\mu_i, \sigma)$ .

- `qi$fd`: the simulated first difference in the simulated expected values for the values specified in `x` and `x1`.
- `qi$att.ev`: the simulated average expected treatment effect for the treated from conditional prediction models.
- `qi$att.pr`: the simulated average predicted treatment effect for the treated from conditional prediction models.

## How to Cite

To cite the *normal* Zelig model:

Kosuke Imai, Gary King, and Oliva Lau. 2007. "normal: Normal Regression for Continuous Dependent Variables" in Kosuke Imai, Gary King, and Olivia Lau, "Zelig: Everyone's Statistical Software," <http://gking.harvard.edu/zelig>

To cite Zelig as a whole, please reference these two sources:

Kosuke Imai, Gary King, and Olivia Lau. 2007. "Zelig: Everyone's Statistical Software," <http://GKing.harvard.edu/zelig>.

Imai, Kosuke, Gary King, and Olivia Lau. (2008). "Toward A Common Framework for Statistical Analysis and Development." *Journal of Computational and Graphical Statistics*, Vol. 17, No. 4 (December), pp. 892-913.

## See also

The *normal* model is part of the *stats* package by Venables and Ripley (2002). Advanced users may wish to refer to `help(glm)` and `help(family)`, as well as McCullagh and Nelder (1989). Robust standard errors are implemented via the *sandwich* package by Zeileis (2004). Sample data are from King et al. (2000).

# Bibliography

- Andrews, D. W. (1991), “Heteroskedasticity and Autocorrelation Consistent Covariance Matrix Estimation,” *Econometrica*, 59, 817–858.
- King, G., Tomz, M., and Wittenberg, J. (2000), “Making the Most of Statistical Analyses: Improving Interpretation and Presentation,” *American Journal of Political Science*, 44, 341–355, <http://gking.harvard.edu/files/abs/making-abs.shtml>.
- Lumley, T. and Heagerty, P. (1999), “Weighted Empirical Adaptive Variance Estimators for Correlated Data Regression,” *jrssb*, 61, 459–477.
- McCullagh, P. and Nelder, J. A. (1989), *Generalized Linear Models*, no. 37 in Monograph on Statistics and Applied Probability, Chapman & Hall, 2nd ed.
- Venables, W. N. and Ripley, B. D. (2002), *Modern Applied Statistics with S*, Springer-Verlag, 4th ed.
- Zeileis, A. (2004), “Econometric Computing with HC and HAC Covariance Matrix Estimators,” *Journal of Statistical Software*, 11, 1–17.